

Given $\alpha = \frac{\sqrt{1+\sqrt{3}}}{\sqrt{5}-4}i - \sqrt[3]{\sqrt{2} + \sqrt[4]{3} - 45}$, find a radical extension $L:\mathbb{Q}$ containing α .