

## Math 199 Study Guide for Final

**Study:** notes, tests, graded homework, homework sheets, old finals

### Main Topics:

Sets and Functions

Mathematical Induction

Equivalence Relations and Partitions

Size of Sets

### Know how to:

state definitions

do graded homework and homework sheet problems

give examples and work examples

show sets are countable or uncountable

### Types of proofs to know:

subset / equality of sets

and / or statements

contradiction

invertibility

equivalence relations

if, then

for all / there exists

1-1 / onto

direct / inverse image

isomorphism

if and only if

contrapositive

irrationality of numbers

induction

countability / uncountability

### Know definitions and terminology:

converse

natural number

real number

union

power set

cartesian product

domain

one-to-one

inverse function

basis for induction

$d$  divides  $n$

the quotient of  $X$  by  $R$

bijection

infinite

contrapositive

integer

irrational number

intersection

even integer

function

codomain

onto

inverse image

induction step

equivalence relation

congruence (mod  $n$ )

isomorphic

countable

contradiction

rational number

subset

difference

odd integer

graph

composition

invertible function

direct image

induction hypothesis

equivalence class

partition

finite

uncountable

### Big Proofs:

Theorem 3:  $\mathbb{Q}$  is countable.

Theorem 4:  $\mathbb{R}$  is uncountable.

**Remark:** The final exam will include a reference page of statements of the major propositions, theorems, and corollaries from the last two weeks of class.